

Terna Engineering College, Nerul.

Dept: -General Engineering.

Sub: Applied Mathematics I

Unit test I (A,B,C,D,E,F,H)

Date:-

Time: 1 hr.

Marks: - 20

Q1. Attempt any five.

Marks 10

- 1) Show that $(1 + i)^{100} + (1 - i)^{100} = -2^{51}$.
- 2) If $\tanh x = \frac{2}{3}$ find $\cosh 2x$.
- 3) Prove that $(\cosh x + \sinh x)^n = \cosh nx + \sinh nx$.
- 4) Prove that $\cosh^{-1}(\sqrt{1 + x^2}) = \tanh^{-1}\left(\frac{x}{\sqrt{1+x^2}}\right)$.
- 5) Find the value of $\log [\sin (x + iy)]$.
- 6) If A is a Hermitian matrix then iA is a skew -Hermitian.
- 7) Find the value of i^i .

Q2. Attempt any one.

Marks 05

- 1) Separate into real and imaginary part $\tan^{-1}(\cos\theta + i\sin\theta)$.
- 2) Solve $x^6 - i = 0$.

Q3. Attempt any one.

Marks 05

- 1) Solve $x^6 - x^5 + x^4 - x^3 + x^2 - x + 1 = 0$.
- 2) Show that every square matrix can be uniquely expressed as $P+iQ$, where P&Q are Hermitian matrices.

-----Best of luck-----